

# Implications of the experimental results on rare $b \rightarrow s + (\gamma, \ell^+ \ell^-)$ decays

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TU Munich – Universe Cluster

7th CKM-Workshop – Cincinnati – 2012

# $\Delta B = 1$ FCNC's: Rich phenomenology ...

$$b \rightarrow s + \gamma$$

$$B \rightarrow K^* \gamma \quad (B_s \rightarrow \phi \gamma)$$

- $Br$
- time-dep. CP asy's:  $S, C, H$
- iso-spin asymmetry  $\Delta_0$

$$B \rightarrow X_s \gamma$$

- $Br, dBr/dE_\gamma$
- $A_{CP}$  in  $B \rightarrow X_s \gamma$  and  $B \rightarrow X_{s+d} \gamma$

$$B_s \rightarrow \gamma \gamma$$

- $Br (A_{CP})$

$$b \rightarrow s + \ell^+ \ell^-$$

$$B_s \rightarrow \ell^+ \ell^- : Br$$

$$B \rightarrow K \ell^+ \ell^- : dBr/dq^2, A_{FB}(q^2), F_H(q^2)$$

$$B \rightarrow K^* (\rightarrow K \pi) \ell^+ \ell^- \quad (B_s \rightarrow \phi (\rightarrow K \bar{K}) \ell^+ \ell^-)$$

$$- dBr/dq^2, A_{FB}(q^2), F_{L,T}(q^2), \dots$$

$$- d^4 Br/dq^2 d\cos\theta_\ell d\cos\theta_K d\phi \rightarrow 12 \text{ angular obsv's } J_{1,\dots,9}^{(s,c)}$$

$$\rightarrow \text{optimized obsv's } A_T^{(2,3,4, \text{re}, \text{im})}, P_{1,\dots,6}, H_T^{(1,\dots,5)}$$

$$B \rightarrow X_s \ell^+ \ell^- : dBr/dq^2, A_{FB}(q^2), H_{T,L}(q^2)$$

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... to test short-distance flavor couplings  $C_i$ :

$$i = 7, 7'$$

$$i = 7^{(\prime)}, 9^{(\prime)}, 10^{(\prime)}, S^{(\prime)}, P^{(\prime)}, T(5), \dots$$

BUT need non-perturbative hadronic input:

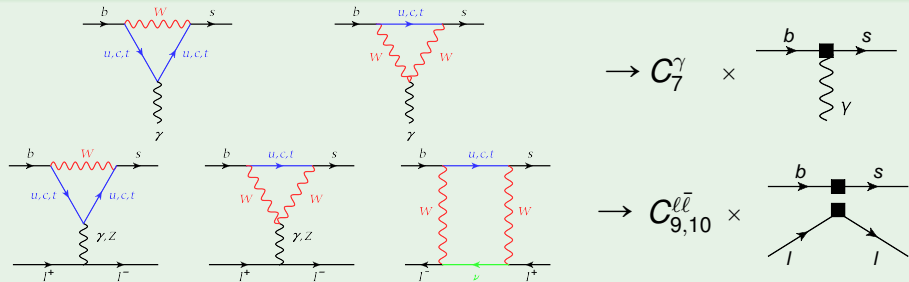
Form factors:  $(B \rightarrow K) \rightarrow f_{+,T,0}$  and  $(B \rightarrow K^*, B_s \rightarrow \phi) \rightarrow V, A_{0,1,2}, T_{1,2,3}$

Decay constants and LCDA's:  $B_{d,s}, K, K^*, \phi, \dots$

Heavy quark expansion parameters:  $\lambda_{1,2}, \dots$ , Shape-functions ...

# EFT (Effective Field Theory) in the SM (Standard Model) for ...

$b \rightarrow s + \gamma$  and  $b \rightarrow s + \ell^+ \ell^-$

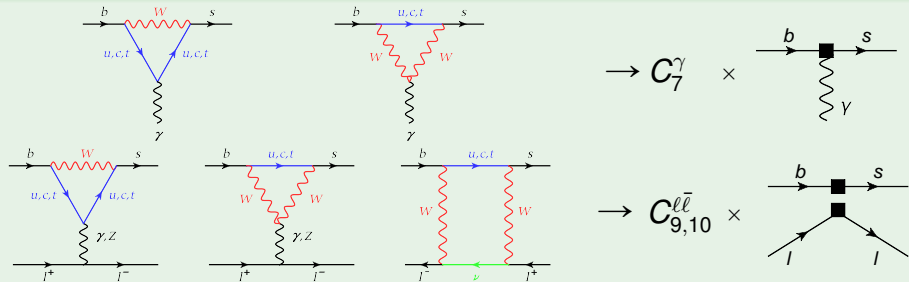


$$O_7^\gamma = \frac{e}{(4\pi)^2} m_b [\bar{s} \sigma^{\mu\nu} P_R b] F_{\mu\nu},$$

$$O_{9,10}^{\ell\bar{\ell}} = \frac{\alpha_e}{4\pi} [\bar{s} \gamma^\mu P_L b] [\bar{\ell} \gamma_\mu (1, \gamma_5) \ell]$$

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and

- current-current op's  $b \rightarrow s + Q\bar{Q}$ , ( $Q = u, c$ )
- QCD penguin op's  $b \rightarrow s + q\bar{q}$ , ( $q = u, d, s, c, b$ )
- chromo-magnetic dipole  $b \rightarrow s + gluon$

$\Rightarrow$  induce backgrounds

$b \rightarrow s + (q\bar{q}) \rightarrow s + \ell^+ \ell^-$

vetoed in exp's for  $q = c: J/\psi$  and  $\psi'$

## More $b \rightarrow s + (\gamma, \ell^+ \ell^-)$ operators beyond the SM ...

... frequently considered in model-(in)dependent searches

**SM'** =  $\chi$ -flipped SM analogues

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**S + P** = scalar + pseudoscalar

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**T + T5** = tensor

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new Dirac-structures beyond SM:

- **SM'** : right-handed currents
- **S + P** : higgs-exchange & box-type diagrams
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## Extension of EFT beyond the SM ...

$$\mathcal{L}_{\text{eff}}(\mu_b) = \mathcal{L}_{\text{QED} \times \text{QCD}}(u, d, s, c, b, e, \mu, \tau, ???) \\ + \frac{4G_F}{\sqrt{2}} V_{\text{CKM}} \sum_{\text{SM}} (C_i + \Delta C_i) \mathcal{O}_i + \sum_{\text{NP}} C_j \mathcal{O}_j(???)$$

⇒  $\Delta C_i$  ... NP contributions to SM  $C_i$

⇒  $\sum_{\text{NP}} C_j \mathcal{O}_j$  ... NP operators (e.g.  $C'_{7,9,10}$ ,  $C'_{S,P}$ , ...)

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# Experimental results

$$B \rightarrow K^* \ell^+ \ell^-$$

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$$B_s \rightarrow \mu^+ \mu^-$$

# Experimental data: $b \rightarrow s \ell^+ \ell^-$ – number of events

# of evts	BaBar 2012 471 M $\bar{B}B$	Belle 2009 605 fb $^{-1}$	CDF 2011 6.8 fb $^{-1}$	LHCb 2011/12 1 fb $^{-1}$
$B^0 \rightarrow K^{*0} \ell \bar{\ell}$	$137 \pm 44^\dagger$	$247 \pm 54^\dagger$	$164 \pm 15$	$900 \pm 34$
$B^+ \rightarrow K^{*+} \ell \bar{\ell}$			$20 \pm 6$	$76 \pm 16$
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- vetoed  $q^2$  region around  $J/\psi$  and  $\psi'$  resonances
- $\dagger$  unknown mixture of  $B^0$  and  $B^\pm$

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[A.J.Bevan arXiv:1110.3901]

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## More details on data

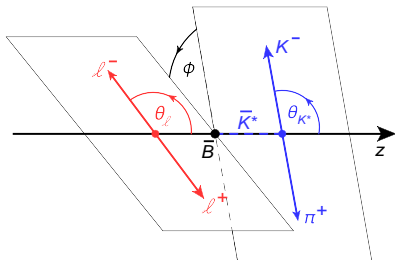
BaBar	Jack RITCHIE	$B \rightarrow K^* \ell^+ \ell^-$	this session
CDF	Satyajit BEHARI	$B \rightarrow K^* \ell^+ \ell^-$	this session
Belle	Cholong LIM	$b \rightarrow s \gamma$	today afternoon session
BaBar	Jack RITCHIE	$b \rightarrow s \gamma$	today afternoon session
LHCb	Flavio ARCHILLI	$B_q \rightarrow \ell^+ \ell^-$	tomorrow session
ATLAS/CMS	Bakul GAUR	$B_q \rightarrow \ell^+ \ell^-$	tomorrow session
CDF	Kevin PITTS	$B_q \rightarrow \ell^+ \ell^-$	tomorrow session



# Angular analysis of $\bar{B} \rightarrow \bar{K}^* [\rightarrow \bar{K}\pi] + \ell^+\ell^-$

4-body decay with on-shell  $\bar{K}^*$  (vector)

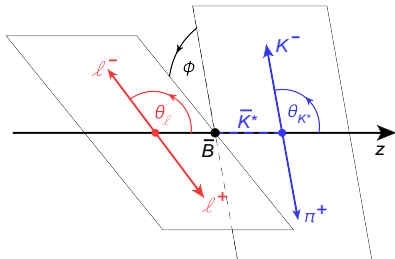
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- 2)  $\cos\theta_\ell$  with  $\theta_\ell \angle(\vec{p}_{\bar{B}}, \vec{p}_\ell)$  in  $(\ell\bar{\ell})$  - c.m. system
- 3)  $\cos\theta_K$  with  $\theta_K \angle(\vec{p}_{\bar{B}}, \vec{p}_{\bar{K}})$  in  $(\bar{K}\pi)$  - c.m. system
- 4)  $\phi \angle(\vec{p}_{\bar{K}} \times \vec{p}_\pi, \vec{p}_{\bar{\ell}} \times \vec{p}_\ell)$  in  $B$ -RF



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$J_i(q^2) = \text{"Angular Observables"}$

$$\frac{32\pi}{9} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = J_{1s} \sin^2\theta_K + J_{1c} \cos^2\theta_K + (J_{2s} \sin^2\theta_K + J_{2c} \cos^2\theta_K) \cos 2\theta_\ell$$

$$+ J_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + J_4 \sin 2\theta_K \sin 2\theta_\ell \cos\phi + J_5 \sin 2\theta_K \sin\theta_\ell \cos\phi$$

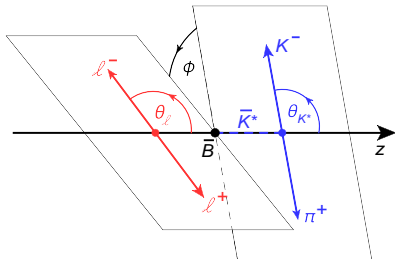
$$+ (J_{6s} \sin^2\theta_K + J_{6c} \cos^2\theta_K) \cos\theta_\ell + J_7 \sin 2\theta_K \sin\theta_\ell \sin\phi$$

$$+ J_8 \sin 2\theta_K \sin 2\theta_\ell \sin\phi + J_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi$$

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$J_i(q^2)$  = "Angular Observables"

$$\frac{32\pi}{9} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = J_{1s} \sin^2\theta_K + J_{1c} \cos^2\theta_K + (J_{2s} \sin^2\theta_K + J_{2c} \cos^2\theta_K) \cos 2\theta_\ell$$

$$+ J_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + J_4 \sin 2\theta_K \sin 2\theta_\ell \cos\phi + J_5 \sin 2\theta_K \sin\theta_\ell \cos\phi$$

$$+ (J_{6s} \sin^2\theta_K + J_{6c} \cos^2\theta_K) \cos\theta_\ell + J_7 \sin 2\theta_K \sin\theta_\ell \sin\phi$$

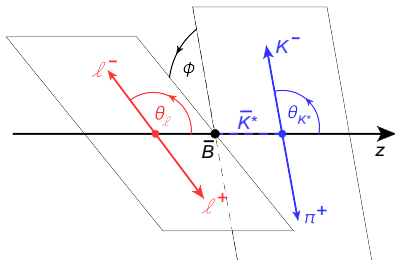
$$+ J_8 \sin 2\theta_K \sin 2\theta_\ell \sin\phi + J_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi$$

$\Rightarrow$  "2  $\times$  (12 + 12) = 48" if measured separately: A) decay + CP-conj and B) for  $\ell = e, \mu$

# Angular analysis of $\bar{B} \rightarrow \bar{K}^* [\rightarrow \bar{K}\pi] + \ell^+ \ell^-$

4-body decay with on-shell  $\bar{K}^*$  (vector)

- 1)  $q^2 = m_{\ell\bar{\ell}}^2 = (p_\ell + p_{\bar{\ell}})^2 = (p_{\bar{B}} - p_{\bar{K}^*})^2$
- 2)  $\cos\theta_\ell$  with  $\theta_\ell \angle(\vec{p}_{\bar{B}}, \vec{p}_\ell)$  in  $(\ell\bar{\ell})$  - c.m. system
- 3)  $\cos\theta_K$  with  $\theta_K \angle(\vec{p}_{\bar{B}}, \vec{p}_{\bar{K}})$  in  $(\bar{K}\pi)$  - c.m. system
- 4)  $\phi \angle(\vec{p}_{\bar{K}} \times \vec{p}_\pi, \vec{p}_{\bar{\ell}} \times \vec{p}_\ell)$  in  $B$ -RF



CP-conj. decay  $B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \ell^+ \ell^-$ :  $d^4\bar{\Gamma}$  from  $d^4\Gamma$  by replacing

$$\text{CP-even} \quad : \quad J_{1,2,3,4,7} \quad \longrightarrow \quad + \bar{J}_{1,2,3,4,7} [\delta_W \rightarrow -\delta_W]$$

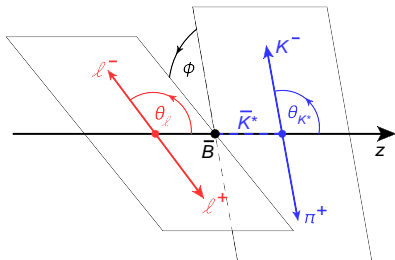
$$\text{CP-odd} \quad : \quad J_{5,6,8,9} \quad \longrightarrow \quad - \bar{J}_{5,6,8,9} [\delta_W \rightarrow -\delta_W]$$

with weak phases  $\delta_W$  conjugated

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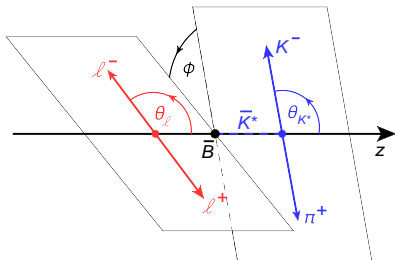
1) CP-odd :  $A_{CP} \sim (J_i - \bar{J}_i) \sim d^4(\Gamma + \bar{\Gamma}) = \text{flavour-untagged } B \text{ samples}$

2) (naive) T-odd  $J_{7,8,9}$ :  $A_{CP} \sim \cos\delta_s \sin\delta_W \rightarrow \text{not suppressed by small strong phases } \delta_s$

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Attention!!! different  $\theta_\ell$  in  $\bar{B} \rightarrow \bar{K}^*$  and  $B \rightarrow K^*$  decays used by Belle, CDF, BaBar:

$$\text{CP-even} : J_{1,2,3,4,5,6} \longrightarrow + \bar{J}_{1,2,3,4,5,6}[\delta_W \rightarrow -\delta_W]$$

$$\text{CP-odd} : J_{7,8,9} \longrightarrow - \bar{J}_{7,8,9}[\delta_W \rightarrow -\delta_W]$$

$\theta_\ell$  between  $\bar{B}$  ( $B$ ) and  $\ell^-$  ( $\ell^+$ ) in  $\bar{B} \rightarrow \bar{K}^*$  ( $B \rightarrow K^*$ )

!!! Not possible in  $\bar{B}_s, B_s \rightarrow \phi(\rightarrow K^+ K^-) \ell^+ \ell^-$  since not self-tagging

Currently, LHCb  $\theta_\ell$  as Belle, CDF, BaBar and  $\phi$  differently for  $\bar{B} \rightarrow \bar{K}^*$  and  $B \rightarrow K^*$

$\Rightarrow$  only CP-even  $J_i$

[LHCb-CONF-2012-008]

Data for  $B \rightarrow K^* + \ell^+ \ell^-$ :  $Br$ ,  $A_{FB}$ ,  $F_L$

angular analysis in each  $q^2$ -bin in  $\theta_\ell$ ,  $\theta_K$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_K} = \frac{3}{2} F_L \cos^2\theta_K + \frac{3}{4} (1 - F_L) \sin^2\theta_K$$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_\ell} = \frac{3}{4} F_L \sin^2\theta_\ell + \frac{3}{8} (1 - F_L) (1 + \cos^2\theta_\ell) + A_{FB} \cos\theta_\ell$$

$\Rightarrow$  fitted  $F_L$  and  $A_{FB}$

# Data for $B \rightarrow K^* + \ell^+ \ell^-$ : $Br, A_{FB}, F_L$

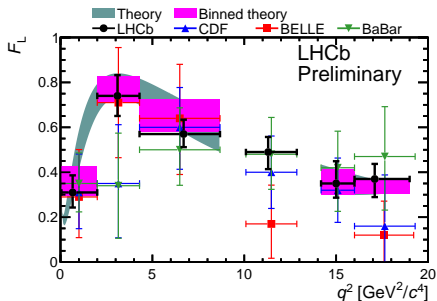
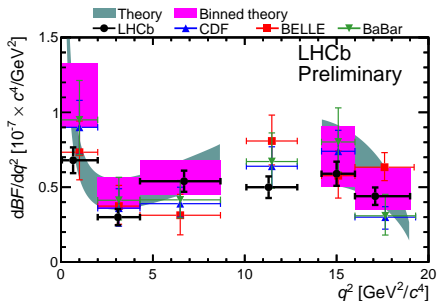
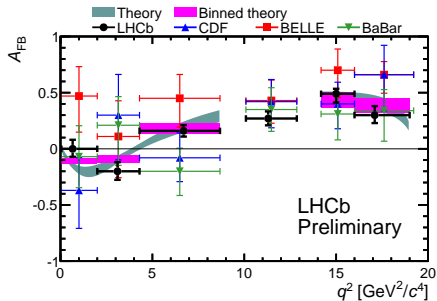
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$\Rightarrow$  fitted  $F_L$  and  $A_{FB}$

SM-predictions: CB/Hiller/van Dyk arXiv:1105.0376  
form factors Ball/Zwicky hep-ph/0412079





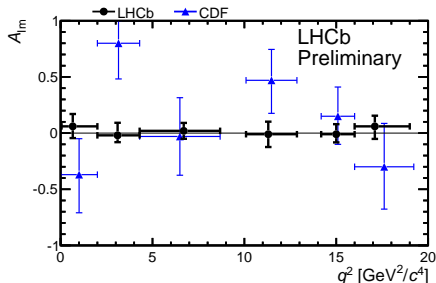
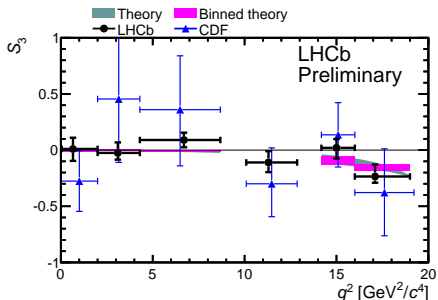
# Data for $B \rightarrow K^* + \ell^+ \ell^-$ :

measurement of  $A_T^{(2)}$ ,  $A_{im}$  from CDF and  $S_3$ ,  $S_9$  from LHCb

$$\frac{2\pi}{(\Gamma + \bar{\Gamma})} \frac{d(\Gamma + \bar{\Gamma})}{d\phi} = 1 + S_3 \cos 2\phi + (A_{im} \text{ or } S_9) \sin 2\phi$$

with

$$S_3 = \frac{J_3 + \bar{J}_3}{\Gamma + \bar{\Gamma}} = \frac{1}{2}(1 - F_L) A_T^{(2)}, \quad A_{im} = A_9 = \frac{J_9 - \bar{J}_9}{\Gamma + \bar{\Gamma}}, \quad S_9 = \frac{J_9 + \bar{J}_9}{\Gamma + \bar{\Gamma}},$$

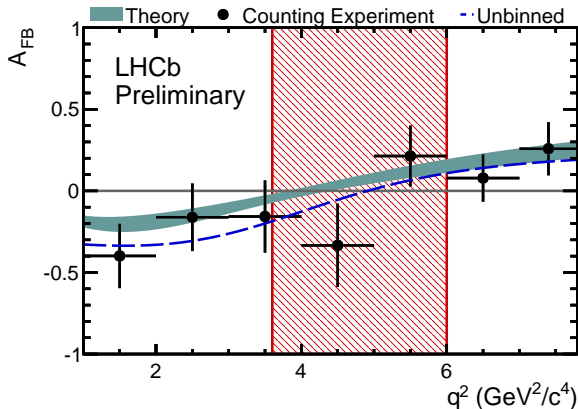


# Data for $B \rightarrow K^* + \ell^+ \ell^-$ :

Zero-crossing of  $A_{FB}$  in low- $q^2$  region:

[LHCb Collaboration LHCb-CONF-2012-008]

finer  $q^2$ -binning than previously: bin-width = 1  $\text{GeV}^2$



Measurement:

$$q_0^2 = (4.9^{+1.1}_{-1.3}) \text{ GeV}^2$$

Theory (SM):

$$q_0^2 = (4.0 \dots 4.3 \pm 0.3) \text{ GeV}^2$$

[Beneke/Feldmann/Seidel hep-ph/0412400]

[Ali/Kramer/Zhu hep-ph/0601034]

[CB/Hiller/van Dyk/Wacker arXiv:1111.2558]

“Optimized observables” in  $B \rightarrow K^* \ell^+ \ell^-$

Not yet measured (except  $A_T^{(2)}$ ) !!!

**Idea:** reduce form factor (FF) sensitivity by combination (usually ratios) of angular obs's  $J_i$   
 $\Rightarrow$  guided by large energy limit @ low- $q^2$  and Isgur-Wise @ high- $q^2$  FF-relations

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@ low- $q^2$  = large recoil

$$A_T^{(2)} = P_1 = \frac{J_3}{2 J_{2s}}, \quad A_T^{(re)} = 2 P_2 = \frac{J_{6s}}{4 J_{2s}}, \quad A_T^{(im)} = -2 P_3 = \frac{J_9}{2 J_{2s}},$$

$$H_T^{(1)} = P_4 = \frac{\sqrt{2} J_4}{\sqrt{-J_{2c}(2J_{2s} - J_3)}}, \quad H_T^{(2)} = P_5 = \frac{J_5/\sqrt{2}}{\sqrt{-J_{2c}(2J_{2s} + J_3)}},$$

$$P_6 = \frac{-J_7/\sqrt{2}}{\sqrt{-J_{2c}(2J_{2s} - J_3)}}, \quad A_T^{(3)} = \sqrt{\frac{(2J_4)^2 + J_7^2}{-2J_{2c}(2J_{2s} + J_3)}}, \quad A_T^{(4)} = \sqrt{\frac{J_5^2 + (2J_8)^2}{(2J_4)^2 + J_7^2}}$$

Krüger/Matias hep-ph/0502060, Egede/Hurth/Matias/Ramon/Reece arXiv:0807.2589 + 1005.0571

[CB/Hiller/van Dyk arXiv:1006.5013](#)

[Becirevic/Schneider arXiv:1106.3283](#)

[Matias/Mescia/Ramon/Virto arXiv:1202.4266](#)

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@ high- $q^2$  = low recoil

$$H_T^{(1)} = P_4 = \frac{\sqrt{2}J_4}{\sqrt{-J_{2c}(2J_{2s} - J_3)}},$$

$$H_T^{(2)} = P_5 = \frac{J_5/\sqrt{2}}{\sqrt{-J_{2c}(2J_{2s} + J_3)}},$$

$$H_T^{(3)} = \frac{J_{6s}/2}{\sqrt{(2J_{2s})^2 - (J_3)^2}},$$

$$H_T^{(4)} = Q = \frac{\sqrt{2}J_8}{\sqrt{-J_{2c}(2J_{2s} + J_3)}},$$

$$H_T^{(5)} = \frac{-J_9}{\sqrt{(2J_{2s})^2 - (J_3)^2}},$$

CB/Hiller/van Dyk arXiv:1006.5013

Matias/Mescia/Ramon/Virto arXiv:1202.4266 + 1207.2753

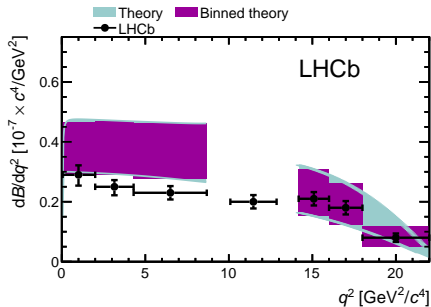
CB/Hiller/van Dyk in preparation, van Dyk PhD-thesis

$B \rightarrow K + \ell^+ \ell^-$ : 3-body decay  $\rightarrow$  2 kinematic variables:  $q^2, \theta_\ell$

$$\frac{1}{(d\Gamma/dq^2)} \frac{d^2\Gamma}{dq^2 d\cos\theta_\ell} = \frac{3}{4} [1 - F_H] \sin^2\theta_\ell + \frac{1}{2} F_H + A_{\text{FB}} \cos\theta_\ell$$

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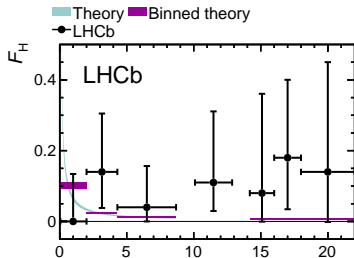
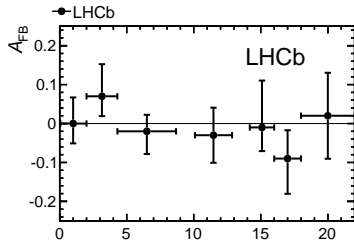
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LHCb arXiv:1209.4284 :  $\langle Br \rangle$ ,  $\langle A_{FB} \rangle$ ,  $\langle F_H \rangle$

and previous results for  $\langle Br \rangle$  from [Belle](#) arXiv:0904.0770  
[CDF](#) arXiv:1107.3753  
[BaBar](#) arXiv:1204.3933

SM prediction: CB/Hiller/van Dyk/Wacker arXiv:1111.2558  
 form factors from Khodjamirian et al. arXiv:1006.4945



## Remark on form factors (FF)

Currently, **FF only known from LCSR @ low  $q^2$**

⇒ @ high  $q^2$  only extrapolations based on some  $q^2$ -dependence

- pole approximations

Ball/Zwicky hep-ph/0406232 + 0412079

- series expansion (z-expansion)

Bharucha/Feldmann/Wick arXiv:1004.3249,

Khodjamirian/Mannel/Pivovavrov/Wang arXiv:1006.4945

@ high  $q^2$ : **Lattice QCD required** to use observables

like  $Br$ ,  $A_{FB}$ ,  $F_L$ ,  $F_H$ , ...

⇒ in progress → see talk by Ran ZHOU this session



$$B_s \rightarrow \mu^+ \mu^-$$

SM prediction:  $Br[B_s \rightarrow \mu^+ \mu^-] \approx 3.5 \times 10^{-9}$

[De Bruyn et al. arXiv:1204.1737]

time-integrated accounting for  $B_s$ -mixing

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Beyond SM:

$$Br \sim \left| \frac{C_S - C'_S}{m_b + m_s} \right|^2 + \left| \frac{C_P - C'_P}{m_b + m_s} + \frac{2m_\ell}{m_{B_s}^2} (C_{10} - C'_{10}) \right|^2$$

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- since  $\sim 10$  years CDF and DØ lowered upper bound from:

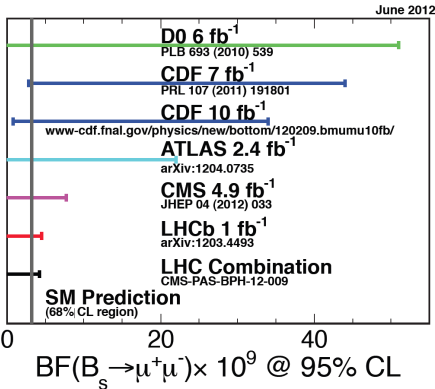
$$\mathcal{O}(10^{-6}) \rightarrow \mathcal{O}(10^{-8})$$

- nowadays measurements from:  
CDF, DØ, LHCb, ATLAS and CMS

$\Rightarrow$  LHC Combination @ 95% CL

= LHCb + ATLAS + CMS

$$Br[B_s \rightarrow \mu^+ \mu^-] < 4.2 \times 10^{-9}$$



# Implications

– Model-independent –

“Global Fit” = combination of  $b \rightarrow s + (\gamma, l^+l^-)$  observables

Parameters of interest

$$\vec{\theta} = (C_i)$$

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Nuisance parameters

1) process-specific

FF's, decay const's,  
LCDA pnr's,  
sub-leading  $\Lambda/m_b$ ,  
renorm. scales:  $\mu_{b,0}$

$\vec{v}$

2) general

quark masses, CKM, ...

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Observables

1) observables

$$O(\vec{\theta}, \vec{v})$$

depend usually on sub-set of  $\vec{\theta}$  and  $\vec{v}$

2) experimental data for each observable

$$\text{pdf}(O = o)$$

$\Rightarrow$  probability distribution of values  $o$

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Fit strategies: 1) Put theory uncertainties in likelihood:

● sample  $\vec{\theta}$ -space (grid, Markov Chain, importance sampling...)

$$\chi^2 = \sum \frac{(O_{\text{ex}} - O_{\text{th}})^2}{\sigma_{\text{ex}}^2 + \sigma_{\text{th}}^2}$$

● theory uncertainties of  $O_i$  at each  $(\vec{\theta})_i$ : vary  $\vec{v}$  within some ranges  $\Rightarrow \sigma_{\text{th}}(O[(\vec{\theta})_i])$

● use Frequentist or Bayesian method  $\Rightarrow$  68 & 95 % (CL or probability) regions of  $\vec{\theta}$



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Fit strategies: 2) Fit also nuisance parameters:

- sample  $(\vec{\theta} \times \vec{v})$ -space (grid, Markov Chain, importance sampling...)
- accounts for theory uncertainties by fitting also  $(\vec{v})_i$
- use Frequentist or Bayesian method  $\Rightarrow$  68 & 95 % (CL or probability) regions of  $\vec{\theta}$  and  $\vec{v}$

# SM basis + real $C_{7,9,10}(4.2 \text{ GeV})$

## 2D marginalised posterior

[Beaujean/CB/van Dyk/Wacker arXiv:1205.1838]

→ individual constraints at 95 % CR from

$B \rightarrow K^* \gamma$  and

# SM basis + real $C_{7,9,10}(4.2 \text{ GeV})$

## 2D marginalised posterior

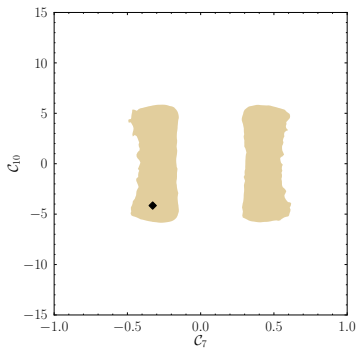
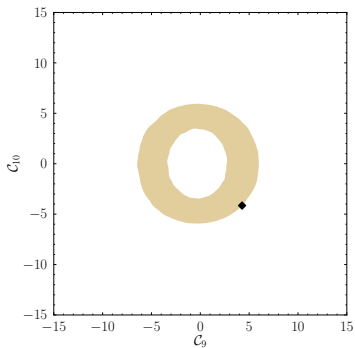
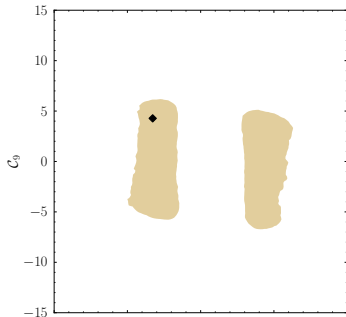
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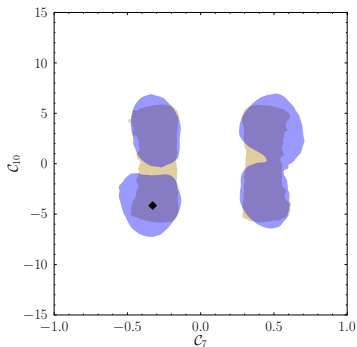
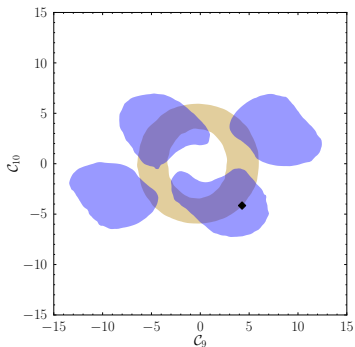
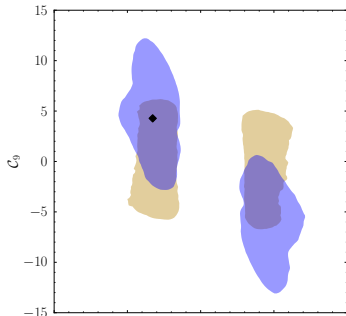
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$$B \rightarrow K^* \gamma$$

and

$$\text{lo+hi-}q^2 B \rightarrow K \ell \bar{\ell}$$

$$\text{lo-}q^2 B \rightarrow K^* \ell \bar{\ell}$$



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[Beaujean/CB/van Dyk/Wacker arXiv:1205.1838]

→ individual constraints at 95 % CR from

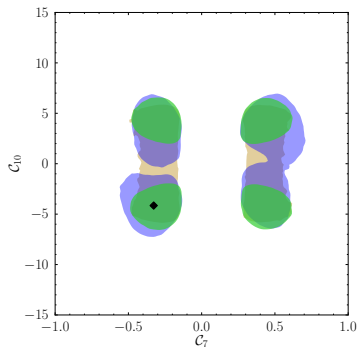
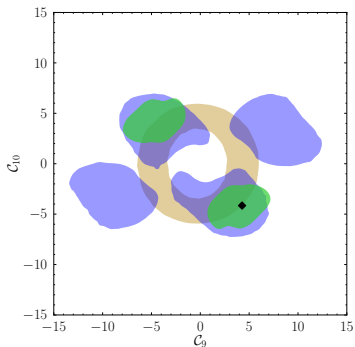
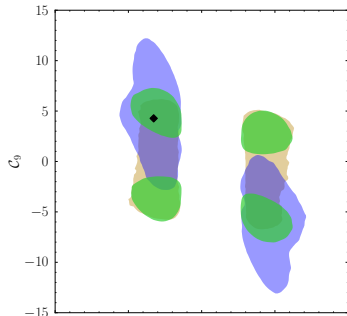
$$B \rightarrow K^* \gamma$$

and

$$\text{lo+hi-}q^2 B \rightarrow K \ell \bar{\ell}$$

$$\text{lo-}q^2 B \rightarrow K^* \ell \bar{\ell}$$

$$\text{hi-}q^2 B \rightarrow K^* \ell \bar{\ell}$$



# SM basis + real $C_{7,9,10}(4.2 \text{ GeV})$

## 2D marginalised posterior

[Beaujean/CB/van Dyk/Wacker arXiv:1205.1838]

→ individual constraints at 95 % CR from

$$B \rightarrow K^* \gamma$$

and

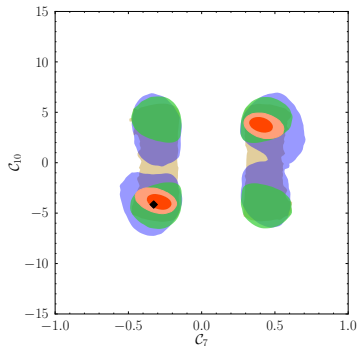
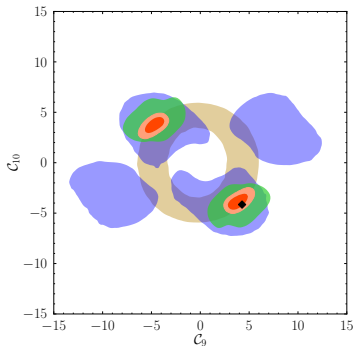
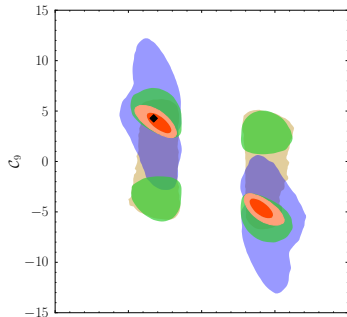
$$\text{lo+hi-}q^2 B \rightarrow K \ell \bar{\ell}$$

$$\text{lo-}q^2 B \rightarrow K^* \ell \bar{\ell}$$

$$\text{hi-}q^2 B \rightarrow K^* \ell \bar{\ell}$$

all constraints (+  $B_s \rightarrow \mu \bar{\mu}$ ):

68 % (95 %) CR



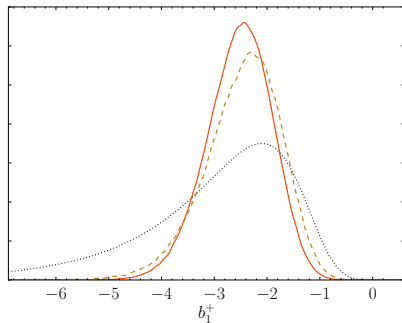
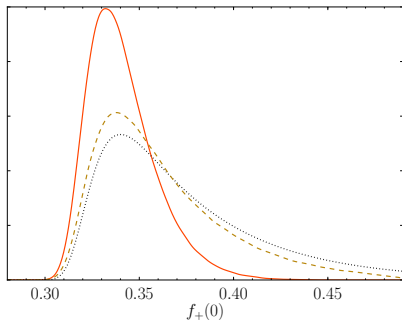
## Nuisance parameter – example $B \rightarrow K$ form factor $f_+(q^2)$

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{\text{res},+}^2} \left[ 1 + b_1^+ \left( z(q^2) - z(0) + \frac{1}{2} [z(q^2)^2 - z(0)^2] \right) \right],$$

$$z(s) = \frac{\sqrt{\tau_+ - s} - \sqrt{\tau_+ - \tau_0}}{\sqrt{\tau_+ - s} + \sqrt{\tau_+ - \tau_0}},$$

$$\tau_0 = \sqrt{\tau_+} (\sqrt{\tau_+} - \sqrt{\tau_+ - \tau_-}),$$

$$\tau_{\pm} = (M_B \pm M_K)^2$$



⇒ Prior [dotted] from LCSR calculation Khodjamirian/Mannel/Pivovarov/Wang arXiv:1006.4945

⇒ Posterior of  $f_+(0)$  [left] and  $b_1^+$  [right] using

1)  $B \rightarrow K \ell^+ \ell^-$  data only [dashed] vs 2) all data [solid, red]

⇒ based on MCMC + Bayesian inference

⇒ included data from

- $B \rightarrow X_s \gamma : Br, A_{CP},$   
 $B \rightarrow K^* \gamma : S$
- $B \rightarrow X_s \ell \bar{\ell} : Br,$   
 $B \rightarrow K \ell \bar{\ell} : Br,$   
 $B \rightarrow K^* \ell \bar{\ell} : Br, A_{FB}, F_L, S_3, A_{im},$   
 $B_s \rightarrow \mu \bar{\mu} : Br$



⇒ based on MCMC + Bayesian inference

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- $B \rightarrow X_s \gamma : Br, A_{CP},$   
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 $B \rightarrow K^* \ell \bar{\ell} : Br, A_{FB}, F_L, S_3, A_{im},$   
 $B_s \rightarrow \mu \bar{\mu} : Br$

⇒ model-indep. NP (real or complex)

- $C_{7,7'}, 9,9', 10,10'$  (in varying stages)
- Z-penguin +  $C_{7,7'}$   
⇒ relates  $b \rightarrow s \ell \bar{\ell}$  and  $b \rightarrow s \nu \bar{\nu}$
- $(C_S - C_{S'}), (C_P - C_{P'})$

here in 2 parameter scenarios  
from arXiv:1206.0273  $\Rightarrow$

$\Rightarrow$  individual constraints at 95 %

$$S[B \rightarrow K^* \gamma]$$

$$Br[B \rightarrow X_S \gamma], A_{CP}[B \rightarrow X_S \gamma]$$

$$Br[B \rightarrow X_S \ell^+ \ell^-]$$

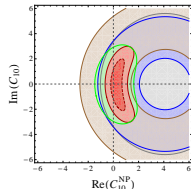
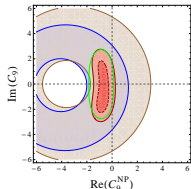
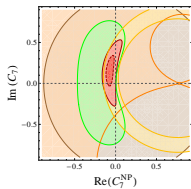
$$B \rightarrow K \ell^+ \ell^-$$

$$B \rightarrow K^* \ell^+ \ell^-$$

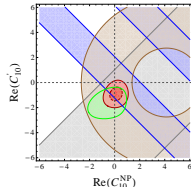
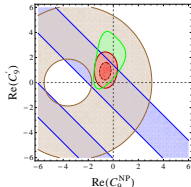
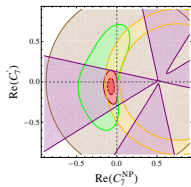
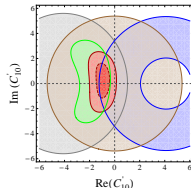
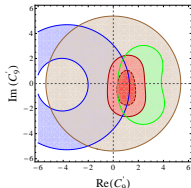
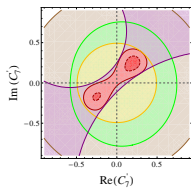
$$B_S \rightarrow \mu^+ \mu^-$$

comb. constraints: 68 % (95 %)

## SM operators:



## chirality-flipped operators:



and update in

Altmannshofer/Straub  
arXiv:1206.0273

⇒ predictions of unmeasured  
observables

- still large T-odd  
CP-asymmetries

at low- $q^2$ :

$$| \langle A_7 \rangle_{[1,6]} | < 35 \%$$

$$| \langle A_8 \rangle_{[1,6]} | < 21 \%$$

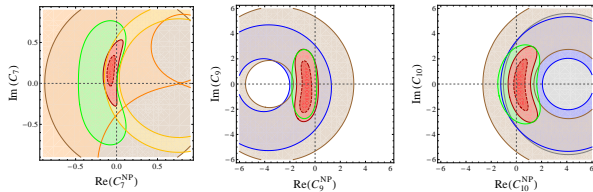
$$| \langle A_9 \rangle_{[1,6]} | < 13 \%$$

at high- $q^2$ :

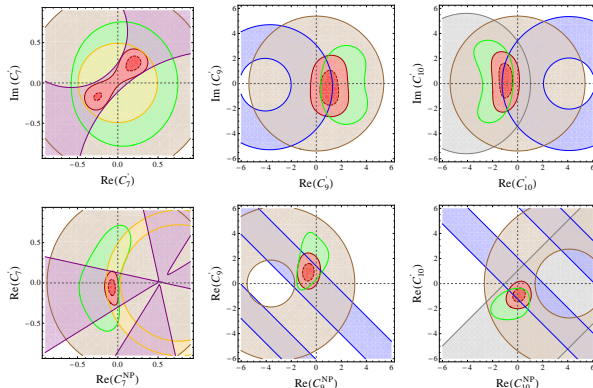
$$| \langle A_8 \rangle_{[14,16]} | < 12 \%$$

$$| \langle A_9 \rangle_{[14,16]} | < 20 \%$$

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Operator	$\Lambda$ [TeV] for $ c_i  = 1$			
	+	-	+i	-i
$\mathcal{O}_7 = \frac{m_b}{e} (\bar{s}\sigma_{\mu\nu} P_R b) F^{\mu\nu}$	69	270	43	38
$\mathcal{O}'_7 = \frac{m_b}{e} (\bar{s}\sigma_{\mu\nu} P_L b) F^{\mu\nu}$	46	70	78	47
$\mathcal{O}_9 = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell)$	29	64	21	22
$\mathcal{O}'_9 = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell)$	51	22	21	23
$\mathcal{O}_{10} = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell)$	43	33	23	23
$\mathcal{O}'_{10} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma_5 \ell)$	25	89	24	23
$\mathcal{O}'_S = \frac{m_b}{m_{B_s}} (\bar{s} P_{R(L)} b)(\bar{\ell}\ell)$	93	93	98	98
$\mathcal{O}_P = \frac{m_b}{m_{B_s}} (\bar{s} P_R b)(\bar{\ell}\gamma_5 \ell)$	173	58	93	93
$\mathcal{O}'_P = \frac{m_b}{m_{B_s}} (\bar{s} P_L b)(\bar{\ell}\gamma_5 \ell)$	58	173	93	93

Lower bounds (at 95% C.L.) on the NP scale  $\Lambda$  of dim-6 op's,  
assuming  $c_i = (+1, -1, +i, -i)$  in (single-operator scenario)

$$H_{\text{eff}} = \frac{c_i}{\Lambda^2} \mathcal{O}_i$$

## Optimized observables $B \rightarrow K^* l^+ l^-$ @ low $q^2$ ...

... experiments provide only  $A_{\text{FB}}, F_L, S_3$ , however optimized observables related as:

$$A_T^{(2)} = P_1 = \frac{2 S_3}{1 - F_L}, \quad A_T^{(re)} = 2P_2 = -\frac{4}{3} \frac{A_{\text{FB}}}{(1 - F_L)}$$

convert  $A_{\text{FB}}, F_L, S_3 \rightarrow P_1, P_2$

[Descotes-Genon/Matias/Ramon/Virto arXiv:1207.2753]

in  $q^2$ -bins: [2, 4.3] and [4.3, 8.68]  $\text{GeV}^2$  (naive theorist conversion due to lacking correlations)

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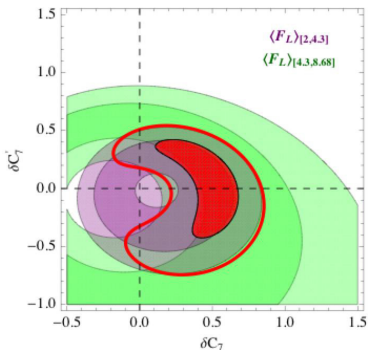
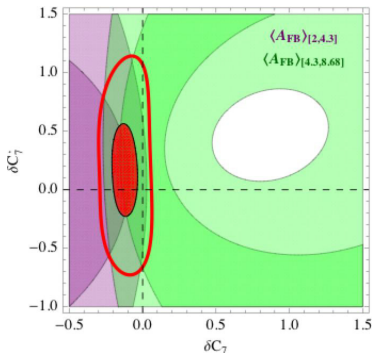
in  $q^2$ -bins: [2, 4.3] and [4.3, 8.68]  $\text{GeV}^2$  (naive theorist conversion due to lacking correlations)

in  $\delta C_7 - \delta C_7'$  plane

$A_{\text{FB}}$

and

$F_L$



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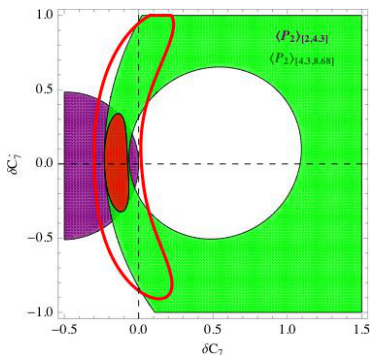
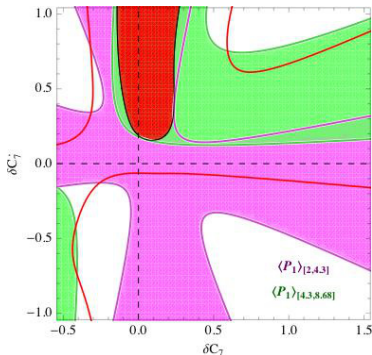
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in  $\delta C_7 - \delta C_7'$  plane

$P_1$

and

$P_2$



# Relation $B_s \rightarrow \mu^+ \mu^-$ and $B \rightarrow K \ell^+ \ell^-$ interesting because ...

⇒ complementary dependence of

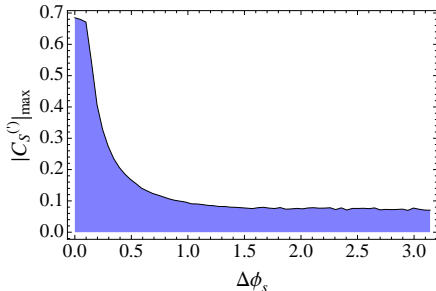
$$B_s \rightarrow \mu^+ \mu^- \rightarrow (C_i - C'_i) \quad \text{for } i = 10, S, P$$

$$B \rightarrow K \ell^+ \ell^- \rightarrow (C_i + C'_i) \quad \text{for } i = 7, 9, 10, S, P$$

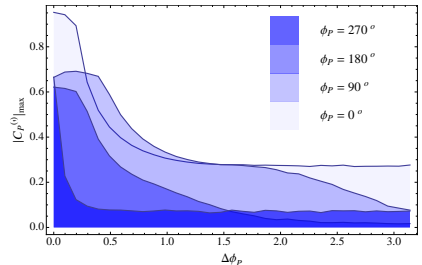
⇒ to constrain scalar and pseudo-scalar operators

⇒  $B \rightarrow K \ell^+ \ell^-$  ( $A_{FB}, F_H$ ) constrain also  $T, T5$

Only complex  $C_{S,S'}$  with relative phase  $\Delta\phi_S$



Only complex  $C_{P,P'}$  with relative phase  $\Delta\phi_P$  and phase  $\phi_P$  of  $C_P$



[Becirevic/Kosnik/Mescia/Schneider arXiv:1205.5811]



## Further analysis based on new data

### Model-independent

- Becirevic/Kou/Le Yaounac/Tayduganov arXiv:1206.1502
- Hurth/Mahmoudi arXiv:1207.0688
- Descotes-Genon/Matias/Ramon/Virto arXiv:1207.2753

### Model-dependent

- Behring/Gross/Hiller/Schacht arXiv:1205.1500
- Mahmoudi/Neshatpour/Orloff arXiv:1205.1845
- Kosnik arXiv:1206.2970

## Implications Summary

- **latest results** of Belle, CDF, Babar, LHCb, CMS and ATLAS on rare  $B \rightarrow (K, K^*)\ell^+\ell^-$  and  $B_s \rightarrow \mu^+\mu^-$  **consistent with SM**:
  - ⇒ two solutions for  $C_{7,9,10}$ : SM-like sign and sign-flipped
    - $B \rightarrow X_s\gamma$  or other obs. sensitive to eff. part of  $C_{7,9}^{\text{eff}}$  might resolve this
  - ⇒  $Br(B \rightarrow K\mu^+\mu^-)$  @ low- $q^2$  lower than SM
- beyond SM:
  - ⇒  $B_s \rightarrow \mu^+\mu^-$  puts stronger constraints on  $C_{S,P}^{(\prime)}$
  - ⇒  $B_s \rightarrow \mu^+\mu^-$  and  $B \rightarrow K\mu^+\mu^-$  constrain  $(C_{9,10} \pm C'_{9,10})$

!!! Currently measured only obs's with rather large theory uncertainties

EOS = Flavour tool @ TU Dortmund by Danny van Dyk et al.

Download @ <http://project.het.physik.tu-dortmund.de/eos/>

## Outlook

- **new  $b \rightarrow s + (\gamma, \ell^+ \ell^-)$  data** from LHCb, CMS, ATLAS
  - ⇒ LHCb additional  $2.2 \text{ fb}^{-1}$  to analyze by the end of 2012
  - ⇒ CMS and ATLAS add.  $\gtrsim 15 \text{ fb}^{-1}$  in 2012 to search for  $B_s \rightarrow \mu^+ \mu^-$
  - and from 2nd generation Flavor-factories Belle II, SuperB  $\gtrsim 2020$
- **first measurements of optimized observables**
  - in exclusive  $B \rightarrow K^*(\rightarrow K\pi)\ell^+\ell^-$  @ low- and high- $q^2$
  - ⇒ combinations with **small hadronic uncertainties**
- first lattice results of form factors  $B \rightarrow K$  and  $B \rightarrow K^*$ 
  - @ high- $q^2$  should become available

– Backup Slides –

## Remark on $Br[B_s \rightarrow \mu^+ \mu^-]$

So far theorists neglected mixing of  $B_s \Rightarrow$  predict  $Br$  at  $t = 0$ :  $Br[B_s(t = 0) \rightarrow \bar{\mu}\mu]$

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But with new measurements of  $\Delta\Gamma_s$  (incl. sign) from LHCb and CDF, DØ

$\Rightarrow$  experiments actually measure **time-integrated  $Br$** :

[De Bruyn et al. arXiv:1204.1737]

$$\begin{aligned} Br[B_s \rightarrow \bar{\mu}\mu] &\equiv \frac{1}{2} \int_0^\infty dt \left( \Gamma[B_s(t) \rightarrow \bar{\mu}\mu] + \Gamma[\bar{B}_s(t) \rightarrow \bar{\mu}\mu] \right) \\ &= \frac{1 + y_s \cdot \mathcal{A}_{\Delta\Gamma}}{1 - y_s^2} Br[B_s(t = 0) \rightarrow \bar{\mu}\mu] \end{aligned}$$

with (LHCb '11)

and

$$y_s = \frac{\Delta\Gamma_s}{2\Gamma_s} = 0.088 \pm 0.014$$

$\Rightarrow$  in SM  $\mathcal{A}_{\Delta\Gamma}|_{\text{SM}} = +1$

$\Rightarrow$  beyond  $\mathcal{A}_{\Delta\Gamma} \in [-1, +1] \rightarrow$  depends on NP !!!

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In SM for example

largest uncertainties from

$$Br[B_s \rightarrow \bar{\mu}\mu]_{\text{SM}} = (3.53 \pm 0.38) \times 10^{-9}$$

$$f_{B_s} = (234 \pm 10) \text{ MeV} \rightarrow 9\%$$

$$V_{ts} \rightarrow 5\%$$

$$B_s \text{ lifetime} \rightarrow 2\%$$

[Mahmoudi/Neshatpour/Orloff arXiv:1205.1845]

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... or using precise  $\Delta M_s$  measurement to substitute  $f_{B_s}$  (and assuming SM) [Buras hep-ph/0303060]

$$Br[B_s \rightarrow \bar{\mu}\mu]_{\text{SM}} = \frac{(3.1 \pm 0.2) \times 10^{-9}}{0.91 \pm 0.01} = (3.4 \pm 0.2) \times 10^{-9}$$

[Buras/Girrbach arXiv:1204.5064]



sgn( $C_7, C_9, C_{10}$ )	best-fit-point	log(MAP)	goodness-of-fit				log( $Z$ )
			$T_{\text{like}}$	$\rho_{\text{like}}$	$T_{\text{pull}}$	$\rho_{\text{pull}}$	
(-, +, -)	(-0.295, 3.73, -4.14)	424.31	402.40	59%	48.8	74%	385.1
(+, -, +)	(0.418, -4.64, 3.99)	424.20	402.32	58%	48.9	74%	385.0
(-, -, +)	(-0.392, -3.09, 3.19)	403.72	387.70	0.8%	76.8	3%	363.8
(+, +, -)	(0.557, 2.25, -3.24)	399.70	384.66	0.2%	82.9	1%	360.1
SM: (-, +, -)	(-0.327, 4.28, -4.15)	430.56 <sup>†</sup>	402.30	69%	49.0	82%	392.4

MAP = maximum a posteriori

$Z$  = local evidence =  $\int d\vec{\theta} d\vec{\nu} P(D|\theta, \nu) \cdot P(\theta, \nu)$  = “likelihood  $\times$  prior”

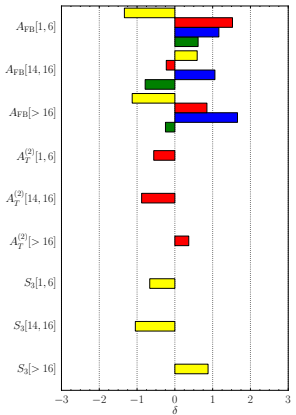
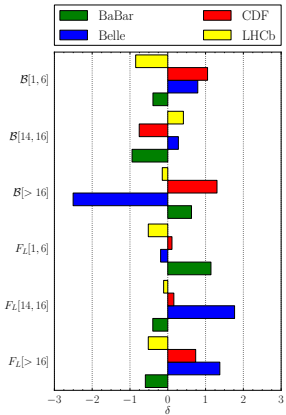
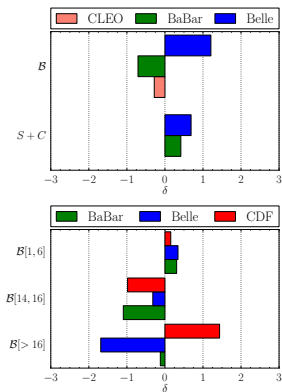
$\Rightarrow$  2 methods to derive  $p$ -values from 2 statistics  $T_{\text{like}}$  and  $T_{\text{pull}}$ :

indicate good fit:  $p \sim (60 - 75)\%$

$\Rightarrow$  model comparison: SM = fixed values of Wilson coefficients  $\Leftrightarrow$  SM-like solution

Bayes factor:  $B = \exp(392.4 - 385.1) \approx 1500$  in favor of the simpler model

22 observables with 59 measurements:  $B \rightarrow K^* \gamma$ ,  $B \rightarrow K \ell^+ \ell^-$ ,  $B \rightarrow K^* \ell^+ \ell^-$



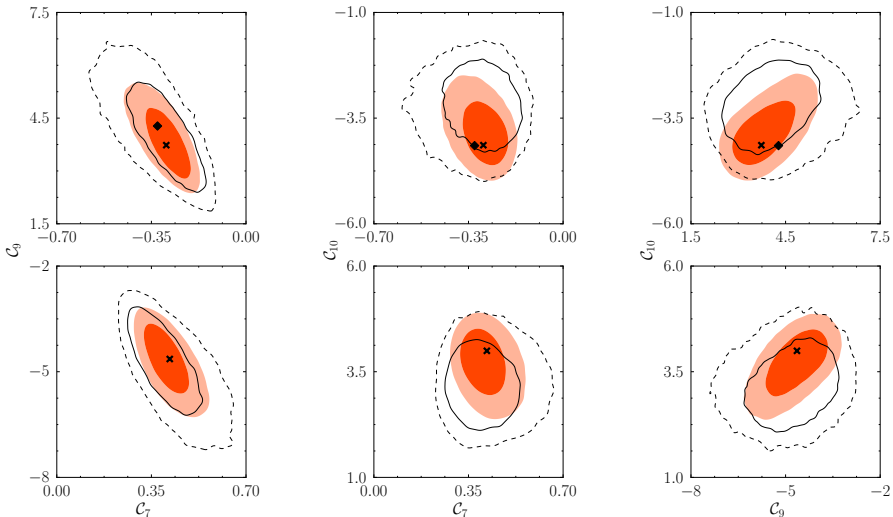
pull definition

$$\delta = \frac{x_{pred}(\vec{\theta}, \vec{v}) - x}{\sigma}$$

- $x_{pred}(\vec{\theta}, \vec{v})$  theory prediction at best fit point
- $x$  central value of experimental distribution
- $\sigma$  experimental uncertainty

# Prior dependence

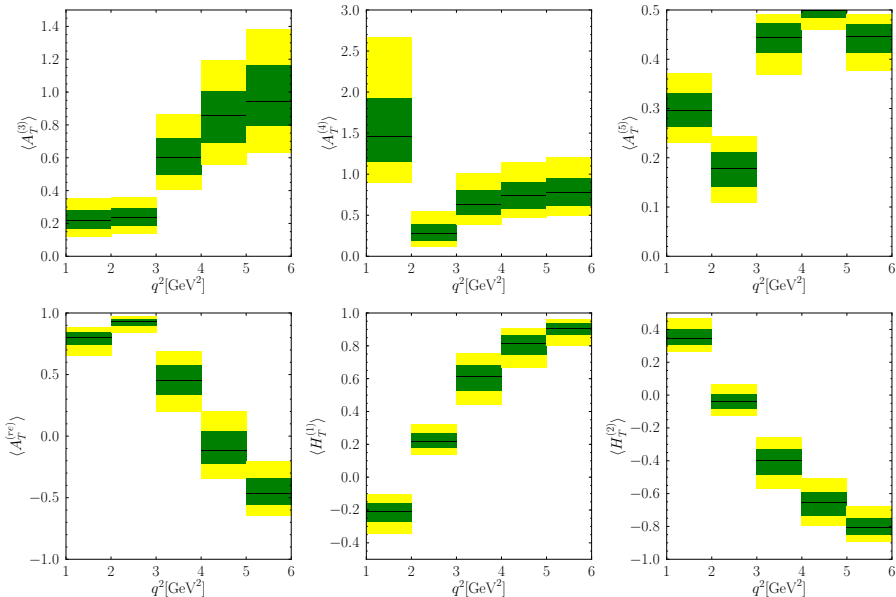
SM = ( $\blacklozenge$ ), best fit point = ( $\times$ )



95 % (dashed) and 68 % (solid) credibility regions using 3 $\times$  larger prior ranges

$\Rightarrow$  fit still converges

# Prediction of yet unmeasured optimized observables @ low- $q^2$



⇒ Measurements outside these predictions would put simple scenario  $C_{7,9,10}$  in trouble

# Low- $q^2$ = Large Recoil

## QCD Factorisation (QCDF)

[Beneke/Feldmann/Seidel hep-ph/0106067, hep-ph/0412400]

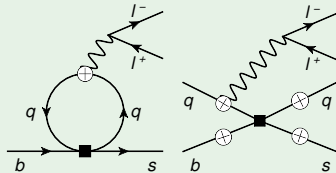
= (large recoil + heavy quark) limit [also Soft Collinear ET (SCET)]

$$\langle \bar{\ell} \ell K_a^* | H_{\text{eff}}^{(i)} | B \rangle \sim$$

$$C_a^{(i)} \times \xi_a + \phi_B \otimes T_a^{(i)} \otimes \phi_{a,K^*} + \mathcal{O}(\Lambda_{\text{QCD}}/m_b)$$

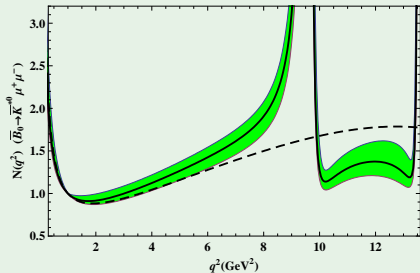
$C_a^{(i)}, T_a^{(i)}$ : perturbative kernels in  $\alpha_s$  ( $a = \perp, \parallel$ ,  $i = u, t$ )

$\phi_B, \phi_{a,K^*}$ :  $B$ - and  $K_a^*$ -distribution amplitudes



## $\bar{c}\bar{c}$ -contributions

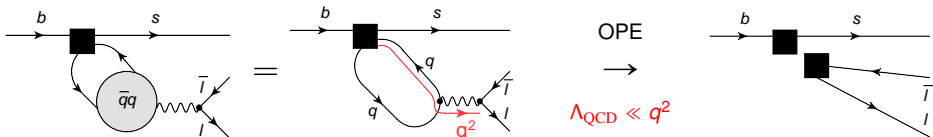
[Khodjamirian/Mannel/Pivovarov/Wang arXiv:1006.4945]



- OPE near light-cone incl. soft-gluon emission (non-local operator) for  $q^2 \leq 4 \text{ GeV}^2 \ll 4m_c^2$
- hadronic dispersion relation using measured  $B \rightarrow K^{(*)}(\bar{c}c)$  amplitudes at  $q^2 \geq 4 \text{ GeV}^2$
- $B \rightarrow K^{(*)}$  form factors from LCSR
- up to (15-20) % in rate for  $1 < q^2 < 6 \text{ GeV}^2$

## High- $q^2 = \text{Low Recoil}$

Hard momentum transfer ( $q^2 \sim M_B^2$ ) through  $(\bar{q}q) \rightarrow \bar{\ell}\ell$  allows local OPE



$$\begin{aligned} \mathcal{M}[\bar{B} \rightarrow \bar{K}^* + \bar{\ell}\ell] &\sim \frac{8\pi^2}{q^2} i \int d^4x e^{iq \cdot x} \langle \bar{K}^* | T \{ \mathcal{L}^{\text{eff}}(0), J_\mu^{\text{em}}(x) \} | \bar{B} \rangle [\bar{\ell} \gamma^\mu \ell] \\ &= \left( \sum_a c_{3a} Q_{3a}^\mu + \sum_b c_{5b} Q_{5b}^\mu + \sum_c c_{6c} Q_{6c}^\mu + \mathcal{O}(\text{dim} > 6) \right) [\bar{\ell} \gamma_\mu \ell] \end{aligned}$$

Buchalla/Isidori hep-ph/9801456, Grinstein/Pirjol hep-ph/0404250, Beylich/Buchalla/Feldmann arXiv:1101.5118

Leading  $\text{dim} = 3$  operators:  $\langle \bar{K}^* | Q_{3,a} | \bar{B} \rangle \sim \text{usual } B \rightarrow K^* \text{ form factors } V, A_{0,1,2}, T_{1,2,3}$

$$Q_{3,1}^\mu = \left( g^{\mu\nu} - \frac{q^\mu q^\nu}{q^2} \right) [\bar{s} \gamma_\nu (1 - \gamma_5) b] \quad \rightarrow \quad C_9 \rightarrow C_9^{\text{eff}}, \quad (V, A_{1,2})$$

$$Q_{3,2}^\mu = \frac{im_b}{q^2} q_\nu [\bar{s} \sigma_{\nu\mu} (1 + \gamma_5) b] \quad \rightarrow \quad C_7 \rightarrow C_7^{\text{eff}}, \quad (T_{1,2,3})$$

$dim = 3$   $\alpha_s$  matching corrections are also known

$m_s \neq 0$  2 additional  $dim = 3$  operators, suppressed with  $\alpha_s m_s / m_b \sim 0.5\%$ ,  
NO new form factors

$dim = 4$  absent

$dim = 5$  suppressed by  $(\Lambda_{\text{QCD}}/m_b)^2 \sim 2\%$ ,  
explicit estimate @  $q^2 = 15 \text{ GeV}^2$ :  $< 1\%$

$dim = 6$  suppressed by  $(\Lambda_{\text{QCD}}/m_b)^3 \sim 0.2\%$  and small QCD-penguin's:  $C_{3,4,5,6}$   
spectator quark effects: from weak annihilation

beyond OPE duality violating effects

- based on Shifman model for  $c$ -quark correlator + fit to recent BES data
- $\pm 2\%$  for integrated rate  $q^2 > 15 \text{ GeV}^2$

$\Rightarrow$  OPE of exclusive  $B \rightarrow K^{(*)} \ell^+ \ell^-$  predicts small sub-leading contributions !!!

BUT, still missing  $B \rightarrow K^{(*)}$  form factors @ high- $q^2$   
for predictions of angular observables  $J_i$

# High- $q^2$ : OPE + HQET

Framework developed by Grinstein/Pirjol hep-ph/0404250

- 1) OPE in  $\Lambda_{\text{QCD}}/Q$  with  $Q = \{m_b, \sqrt{q^2}\}$  + matching on HQET + expansion in  $m_c$

$$\mathcal{M}[\bar{B} \rightarrow \bar{K}^* + \bar{\ell}\ell] \sim \frac{8\pi}{q^2} \sum_{i=1}^6 C_i(\mu) \mathcal{T}_\alpha^{(i)}(q^2, \mu) [\bar{\ell}\gamma^\alpha \ell]$$

$$\begin{aligned} \mathcal{T}_\alpha^{(i)}(q^2, \mu) &= i \int d^4x e^{iq \cdot x} \langle \bar{K}^* | T\{\mathcal{O}_i(0), j_\alpha^{\text{em}}(x)\} | \bar{B} \rangle \\ &= \sum_{k \geq -2} \sum_j C_{i,j}^{(k)} \langle \mathcal{Q}_{j,\alpha}^{(k)} \rangle \end{aligned}$$

$\mathcal{Q}_{j,\alpha}^{(k)}$	power	$\mathcal{O}(\alpha_s)$
$\mathcal{Q}_{1,2}^{(-2)}$	1	$\alpha_s^0(Q)$
$\mathcal{Q}_{1-5}^{(-1)}$	$\Lambda_{\text{QCD}}/Q$	$\alpha_s^1(Q)$
$\mathcal{Q}_{1,2}^{(0)}$	$m_c^2/Q^2$	$\alpha_s^0(Q)$
$\mathcal{Q}_{j>3}^{(0)}$	$\Lambda_{\text{QCD}}^2/Q^2$	$\alpha_s^0(Q)$
$\mathcal{Q}_i^{(2)}$	$m_c^4/Q^4$	$\alpha_s^0(Q)$

included,  
unc. estimate by naive pwr cont.

- 2) HQET FF-relations at sub-leading order +  $\alpha_s$  corrections in leading order

$$T_1(q^2) = \kappa V(q^2), \quad T_2(q^2) = \kappa A_1(q^2), \quad T_3(q^2) = \kappa A_2(q^2) \frac{M_B^2}{q^2},$$

$$\kappa = \left( 1 + \frac{2D_0^{(v)}(\mu)}{C_0^{(v)}(\mu)} \right) \frac{m_b(\mu)}{M_B}$$

can express everything in terms of QCD FF's  $V, A_{1,2}$  @  $\mathcal{O}(\alpha_s \Lambda_{\text{QCD}}/Q)$  !!!